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%Title: "A unimodular demand type which is not a basis change of substitutes"
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%For further details, please contact:
             Timothy O'Connor, timothy.oconnor@economics.ox.ac.uk
Elizabeth Baldwin, e.c.baldwin@lse.ac.uk
\$This\ program\ checks\ whether\ or\ not\ there\ exists\ a\ basis\ change\ for\ a\ \$SPECIFIC\ 4x9\ matrix\ whose\ resulting\ basis\ change\ will\ have\ max\ 1\ positive\ and
%max 1 negative entry in each column. As this is for a specific 4x9 matrix, %this program is NOT immediately generalizable for any 4x9 matrix.
%We start by initiliazing all of our variables (1) before finding all
%possible combinations of the first four columns of our 4x9 matrix with %<=2 nonzero entries in (2) and (3). We throw out from consideration any %matrix who would not have the first four columns being invertible (4). (5)
%takes the invertible matrices and fills out the rest of the columns. \$(6),(7), and (8) will filter based on if a matrix generates >2 NZ entries
%(0),(/), and (8) will filter pased on if a matrix generates >2 N2 entries %in the later part of the matrix. (9) throws out any collection of columns %that were originally invertible which are no longer invertible. (10) will %then check to see if the last group of candidate matrices can have at most %1 positive and at most 1 negative entry in each column.
%Notation:
 \ensuremath{^{\circ}}\ensuremath{^{\circ}}\ensuremath{^{\circ}}\ensuremath{^{\circ}}\ensuremath{^{\circ}}\ensuremath{^{\circ}} and the matrix in question
%Dt = full matrix whose columns are the vectors of the demand type
%P = basis change on Dt, so that P.Dt is the matrix that would have at most one positive and at most one negative entry in each column
\ensuremath{\mathtt{\$}}\xspace The unimodular demand type, Dt, that we are investigating is given by:
a=[1,0,0,0];a=a';
c=[0,0,1,0];c=c';
d=[1,0,0,1];d=d';
A=[a,b,c,d];
Dt=[A, d-a+b, d-a+c, d+b, d+c, d-a+b+c];
%% 1. Initialization of the variables/matrices
%We start by creating the possible basis change matrix P by producing symbolic variables
%that are constrained to the reals.
syms pl_1 real pl_2 real pl_3 real pl_4 real p2_1 real p2_2 real p2_3 real p2_4 real p3_1 real p3_2 real p3_3 real p3_4 real p4_1 real p=[p1_1,p1_2,p1_3,p1_4;p2_1,p2_2,p2_3,p2_4;p3_1,p3_2,p3_3,p3_4;p4_1,p4_2,p4_3,p4_4];
\% 2. Initialization of set of matrices with number of nonzero entries <=2
% We gather all possible ways a 4x4 matrix can have at most 2 nonzero entries in each column
% Once we have found them, we will then assume this matrix has the form "PA" and set the remaining entries of PA to zero.
perms=nchoosek(4,2);%Total number of ways to have 2 Nonzero (NZ) entries in a column
perms 1=nchoosek(4,1); %Total number of ways to have 1 NZ entry in a colum
perms_l=nchoosek(4,1);%Total number of ways to have 1 NZ entry in a colum
perm_point=nchoosek((1:4),2);%List of combinations for the 2 NZ selections
perml_point=nchoosek((1:4),1);%List of combinations for the 1 NZ selection
max_perms=perms^4+perms_1*perms^3*4+6*perms^2*perms_1^2+4*perms*perms_1^3+perms_1^4;%total amount of combinations
max_matrix_collection=zeros(4,4,max_perms);%Preallocating space
We collect all the possible matrices with 2 nonzero entries in each column %such that we cycle through perm_point for each column
for i=1:perms
      i_p=perm_point(i,:);
for j=1:perms
             j_p=perm_point(j,:);
for k=1:perms
                    k_n.perms
k_p=perm_point(k,:);
for h=1:perms
h_p=perm_point(h,:);
                           blank z=zeros(4,4);
                           blank z (i p,1)=1; %We input 1 as these will be the locations that are NZ blank z (j p,2)=1;
                           blank_z(k_p, 3) =1;
blank_z(h_p, 4) =1;
                            \begin{tabular}{ll} max_matrix_collection(:,:,n)=blank_z; &Collect the matrix n=n+1; \end{tabular} 
      end
end
                    end
end
%Now we collect all the combinations with 3 columns having 2 nonzero
%entries and 1 column having 1 nonzero entry
%4th column has 1 nonzero
for i=1:perms
      i_p=perm_point(i,:);
for j=1:perms
              j p=perm point(j,:);
              for k=1:perms
                    k_p=perm_point(k,:);
for h=1:perms_1
h_p=perm1_point(h);
                           blank_z=zeros(4,4);%reset
blank_z(i_p,1)=1;
                           blank z(j p, 2) = 1;
blank z(k p, 3) = 1;
blank z(k p, 3) = 1;
blank z(h p, 4) = 1;
max matrix_collection(:,:,n) = blank_z;
n=n+1;
                    end
             end
      end
end
%3rd column has 1 nonzero
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for i=1:perms
        i_p=perm_point(i,:);
for j=1:perms
                  h_p=perm_point(h,:);
blank_z=zeros(4,4);%reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1;
       end
end
%2nd column has 1 nonzero
for i=1:perms
        1=!:perms
ip=perm point(i,:);
for j=!:perms_1
j_p=perm1_point(j);
for k=1:perms
k_p=perm_point(k,:);
                           for h=1:perms
                                  h=1:perms
h_p=perm_point(h,:);
blank_z=zeros(4,4); *reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1:
       end
end
                                   n=n+1;
end
%1st column has 1 nonzero
for i=1:perms_1
    i_p=perm1_point(i);
    for j=1:perms
                  j_p=perm_point(j,:);
for k=1:perms
                           k_p=perm_point(k,:);
for h=1:perms
                                   h_p=perm_point(h,:);
                                   blank_z=zeros(4,4);%reset
blank_z(i_p,1)=1;
                                  blank_z(j_p,2)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1;
       end
end
                          end
Now we collect all the combinations with 2 columns having 2 nonzero entries and 2 columnns having 1 nonzero entry
%1st and 2nd have 1 nonzero
for i=1:perms 1

i p=perm1_point(i);%1st column has 1

for j=1:perms_1

j_p=perm1_point(j);%2nd column has 1

for k=1:perms_int(b, c);
                           k=1:perms
k_p=perm_point(k,:);
for h=1:perms
h_p=perm_point(h,:);
blank_z=zeros(4,4);%reset
blank_z(i_p,1)=1;
                                  blank_z(j_p,z)=1;
blank_z(j_p,z)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n-1;
       end
end
%1st and 3rd have 1 nonzero
for i=1:perms_1

i_p=perm1_point(i);

for j=1:perms
j_p=perm_point(j,:);

for k=1:perms_1

k_p=perm1_point(k);
                           for h=1:perms
                                  h=1:perms
h_perm point(h,:);
blank_z=zeros(4,4); %reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
               end
end
                                   n=n+1;
        end
end
%1st and 4th have 1 nonzero
for i=1:perms_1
    i_p=perm1_point(i);
    for j=1:perms
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j_p=perm_point(j,:);
for k=1:perms
    k_p=perm_point(k,:);
                                                          k_p=perm_point(k,:);
for h=1:perms_1
   h_p=perml_point(h);
   blank_z=zeros(4,4);%reset
   blank_z(i_p,1)=1;
   blank_z(j_p,2)=1;
   blank_z(k_p,3)=1;
   blank_z(h_p,4)=1;
   max_matrix_collection(:,:,n)=blank_z;
   n=p+1;
                                                                              n=n+1;
                end
end
                                                         end
 end
   %2nd and 3rd have 1 nonzero
 for i=1:perms
                   i=::perms
i_p=perm_point(i,:);
for j=1:perms_1
    j_p=perm1_point(j);
    for k=1:perms_1
    k_p=perm1_point(k);
    for h=1:perms
                                                                             h_p=perm_point(h,:);
blank_z=zeros(4,4);%reset
                                                                              blank_z(i_p,1)=1;

blank_z(i_p,2)=1;

blank_z(k_p,3)=1;

blank_z(k_p,3)=1;

blank_z(k_p,4)=1;

max_matrix_collection(:,:,n)=blank_z;
                 end
end
                                                                               n=n+1;
  %2nd and 4th have 1 nonzero
  for i=1:perms
                   1=1:perms
i_p=perm_point(i,:);
for j=1:perms_1
    j_p=perm1_point(j);
    for k=1:perms
                                                           k_nerm_point(k,:);
for h=1:perms_1
    h_p=perm1_point(h);
                                                                              hlank_z=zeros(4,4); %reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
                                                                               max_matrix_collection(:,:,n)=blank_z;
                                                        end
                 end
end
 end
   %3rd and 4th have 1 nonzero
 for i=1:perms
                  i=1:perms
i_p=perm_point(i,:);
for j=1:perms
    j_p=perm_point(j,:);
    for k=1:perms_1
        k_p=perml_point(k);
        for h=1:perms_1
        h_p=perml_point(h);
                                                                             n_pepermi_point(n);
blank_z=zeros(4,4);*reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1:
                                                                              n=n+1;
                                                         end
                                      end
                   end
And\ now\ we\ collect\ all\ the\ combinations\ with\ 3\ columns\ having\ 1\ nonzero\ and\ one\ column\ having\ 2\ nonzero\ entries
  %4th has 2 nonzero
%4th has 2 nonzero
for i=1:perms_1
   i_p=perm1_point(i);
   for j=1:perms_1
   j_p=perm1_point(j);
   for k=1:perms_1
        k_p=perm1_point(k);
        for h=1:perms
        h_p=perm_point(h,:);
        h_p=perm
                                                                            h_p=perm_point(h,:);
blank_z=zeros(4,4);%reset
blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1;
                                    end
end
                   end
  %3rd has 2 nonzero
 for i=1:perms_1
i_p=perm1_point(i);
                   for j=1:perms
j_p=perm_point(j,:);
for k=1:perms_1
    k_p=perm1_point(k);
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for h=1:perms 1
                             h_p=perm1_point(h);
blank_z=zeros(4,4);%reset
                            blank_z(i_p,1)=1;
blank_z(j_p,2)=1;
blank_z(k_p,3)=1;
blank_z(k_p,4)=1;
                             max_matrix_collection(:,:,n)=blank_z;
              end
end
                             n=n+1;
        end
  end
   %2nd has 2 nonzero
  for i=1:perms_1
   i_p=perm1_point(i);
   for j=1:perms_1
        j_p=perm1_point(j);
                for k=1:perms
                      k=1:perms
k_p=perm_point(k,:);
for h=1:perms_1
    h_p=perml_point(h);
    blank_z=zeros(4,4);%reset
    blank_z(i_p,1)=1;
    blank_z(j_p,2)=1;
    blank_z(k_p,3)=1;
    blank_z(h_p,4)=1;
                            blank_z(h_p,4)=1;
max_matrix_collection(:,:,n)=blank_z;
n=n+1;
        end
end
end
                            blank_z(i_p,1)=1;

blank_z(i_p,2)=1;

blank_z(k_p,3)=1;

blank_z(k_p,3)=1;

blank_z(k_p,4)=1;

max_matrix_collection(:,:,n)=blank_z;

n=n+1;
                     end
        end
end
   %Now collect with all four having 1 NZ
   for i=1:perms 1
       i_=-perm_point(i);
for j=1:perms_1
    j_p=perml_point(j);
    for k=1:perms_1
        k_p=perml_point(k);
        for h=1:perms_1
            h_p=perml_point(h);
        blank_z=zeros(4,4);%reset
        blank_z(i_p,1)=1;
        blank_z(i_p,2)=1;
        blank_z(i_p,2)=1;
        blank_z(i_p,4)=1;
        max_matrix_collection(:,:,n)=blank_z;
        n=n+1;
         i_p=perm_point(i);
       end
end
    And now we have all of the matrices
  %Let us now put it into our actual format (with the pi j's)
   %% 3. Now we take the set of matrices and express it in "PA" matrix form.
   %Preallocate space for the combinations of "PA" - Warning, this is where the
   %computing time starts to increase as we loop over symbolic variables
  A_combos= sym(zeros(4,4,max_perms));
  This gets us our "PA" matrix for all the combinations of columns with <=2 %nonzero entries
  for n=1:max_perms
  for i=1:4
         for j=1:4

if (max_matrix_collection(i,j,n)==1)%If this entry is NZ, then input the correct pi_j value
                     A_combos(i,j,n)=dot(p(i,:),A(:,j));
               else
                      A_combos(i,j,n)=0;
               end
         end
     end
  %This makes sure that the appropriate substitutions are in place. If pi_1 % is equal to zero and if pi_1+pi_4 is NZ then we should just have pi_4 by itself
  for n=1:max_perms
for i=1:4
for j=1:3
                      if A_combos(i,j,n)==0
    A_combos(:,:,n)=subs(A_combos(:,:,n),p(i,j),0);
                      end
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end
end
%% 4. Now we filter all the "PA" matrices that would not be invertible
%Preallocating space for our invertible collection
for n=1:max perms
     if rank(A_combos(:,:,n))==4
  count=count+1;
     end
inv A combos= sym(zeros(4,4,count));
count=0;
for n=1:max_perms
if rank[A_combos(:,:,n))==4%If this matrix is invertible, we add it to our list
          count=count+1;
          inv_A_combos(:,:,count)=A_combos(:,:,n);
     end
end
%% 5. Now we fill out our collection to include columns 5:9. That is, we now work with the collection of matrices of the form "P.Dt".
 full_combos=sym(zeros(4,9,count));
for n=1:count
    %From our original matrix, if our first four columns are: a,b,c,d, then:
     \begin{array}{l} c8 = inv \ A \ combos \ (:,4,n) + inv \ A \ combos \ (:,3,n) \ ; \$c8 \ is \ d+c \\ c9 = inv \ A \ combos \ (:,4,n) - inv \ A \ combos \ (:,1,n) + inv \ A \ combos \ (:,2,n) + inv \ A \ combos \ (:,3,n) \ ; \$c9 \ is \ d-a+b+c \\ filling = \ [c5,c6,c7,c8,c9]; \end{array} 
    full_combos(:,:,n)=[inv_A_combos(:,:,n),filling];
%% 6. Now we check the amount of NZ entries in each column.
alive=0; %new count of matrices that "survive" the filter
%We take our set and filter out the matrices with greater than
%2 NZ entries within a column. One important thing to note that if we have
%pi_j, for j=1,2,3, by itself in an entry, we know that it is NZ. However,
*pi_j, for j=1,2,3, by itself in an entry, we know that it is NZ. However, which is not necessarily the case if we have pi_4 by itself. If all that we %know is that pi_1+pi_4 is NZ, this does not tell us whether or not pi_4 is %zero. Therefore, when we count the number of NZ entries in each column, we %can add to our count if we have a pi_j, j~=4, by itself, and pi_4 will %only increase our count if pi_1 is zero.
\$ It is much faster to first count how many matrices will remain after this \$ step, preallocate the required space, and then collect those matrices. Here
\mbox{\ensuremath{\$}} we perform that first count. for k=1:count
     Flag=0;% will flag on if we have more than two nonzero entries in a column. We will then not add that matrix to our next list.
         j=5:9
nz=0;%A counting term for the number of nonzero entries
          for i=1:4
               nz=nz+1;
                    nz=nz+1;
                    elseif full_combos(i,j,k)==full_combos(i,4,k)%If pi_4 is the only entry in the 4th column, then pi_1=0 and so pi_4 is I
               end elseif len>6%We know look for a double that we know would be NZ. The only double that we would know is NZ would be the doul if full_combos(i,j,k)==full_combos(i,4,k)
                         nz=nz+1;
                    end
               end
          end
          if nz>2
               flag=1;
          end
          if full_combos(:,j,k)==[0;0;0;0]%After step five of filling out the rest of the columns, there may be a column with all zeros
               flag=1;
     end
     if flag==0%If we do not have an columns with >2 NZ entries then we increase our count.
        alive=alive+1;
     end
%Now that we have the count, preallocate, then write in data - this next part is the same loop as above, we just write in the data now
first filter num=alive;
first filter=sym(zeros(4,9,first_filter_num));
alive=0;
for k=1:count
     flag=0;
for j=5:9
          nz=0;
          for i=1:4
               str=char(full_combos(i,j,k));
len=length(str);
               if len<6&&len>2
                         nz=nz+1;
                    end
               elseif len>6
if full_combos(i,j,k)==full_combos(i,4,k)
                    end
               end
          end
          if nz>2
               flag=1;
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if full combos(:,i,k) == [0;0;0;0]
                 flag=1;
            end
      end
      if flag==0
         alive=alive+1;
         first_filter(:,:,alive)=full_combos(:,:,k);
\$\$ 7. Now subtitute for the matrices with >2 entries when 2 are for sure NZ
%If a column has for sure 2 nonzero entries and then other entries that are
% not formally set to zero, we can now formally set to zero the other entries that are % entries. For example, the entries in a column are: % [p1_2+p1_4,p2_1,p3_3,p4_2+p2_4]. As the second and third entry are for % sure NZ we can formally set to zero the values of the first and fourth entry (throughout % the entire matrix). Our column is then: [0,p2_1,p3_3,0].
for k=1:first_filter_num
      for j=5:9
            nz=0:
            flag=0;
            for i=1:4
                 1=:4
str=char(first_filter(i,j,k));%As before, we string the entries and inspect the last character. If we have pi_4, then it w.
len=length(str);%Store the location of the last character
if len<66&len>1%If the length is greater than 1 such that it is not "0" and less than 6 such that it is a single element (1
    if str(len)~='4'
                             nz=nz+1:
                        nz=nz+1;
                        end
                 elseif len>6%We know look for a double that we know would be NZ. The only double that we would know is NZ would be the doul
                       end
                 end
            end
            if nz==2
                 flag=1;
            end
            if flag==1
                 %If we have two nonzero entries in this column, we will not go
%back and formally set to zero any entries that we did not
%formally know if they were NZ or not
                       str=char(first_filter(i,j,k));
                       len=length(str); if len>6 && first_filter(i,j,k)~=first_filter(i,4,k)%If this entry is a double and it is NOT the double whose formal v_i
                             first_filter(:,:,k)=subs(first_filter(:,:,k),first_filter(i,j,k),0);%Then we formally set this entry to zero and we set flen<6 &&len>1 && str(len)=='4' && first_filter(i,j,k)~=first_filter(i,4,k)%If the entry is pi_4 where we did not first_filter(:,:,k)=subs(first_filter(:,:,k),first_filter(i,j,k),0);%Then we formally set set pi_4 to zero and we is first_filter(i,j,k).
                        end
           end
     end
%% 8. Now we filter again based on >2 NZ
%After our substitutions made in 7, we once again filter based on a count %of the NZ entries in each column. This step is identical to step 6.
alive=0;
for k=1:first filter num
     flag=0;
for j=5:9
            nz=0:
            for i=1:4
                 str=char(first filter(i,i,k));
                 len=length(str);
if len<6&&len>2
                       if str(len) ~= '4'
                             nz=nz+1;
                       nz=nz+1;
end
                        elseif first_filter(i,j,k) ==first_filter(i,4,k)
                 elseif len>6
   if first filter(i,j,k) == first filter(i,4,k)
                             nz=nz+1;
                       end
                 end
            end
           if nz>2
                 flag=1;
            end
      end
      if flag==0
        alive=alive+1;
      end
second_filter_num=alive;
second_filter=sym(zeros(4,9,second_filter_num));
for k=1:first_filter_num
     flag=0;
for j=5:9
            nz=0:
            for i=1:4
                 str=char(first filter(i,i,k));
                  len=length(str);
                 if len<6&&len>2
                       if str(len) ~= '4'
                        elseif first_filter(i,j,k) == first_filter(i,4,k)
                             nz=nz+1;
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end
                   elseif len>6
   if first_filter(i,j,k) == first_filter(i,4,k)
                               nz=nz+1;
                  end
             end
            if nz>2
                   flag=1;
            end
      end
      if flag==0
         alive=alive+1;
          second_filter(:,:,alive)=first_filter(:,:,k);
      end
end
%% 9. Now filter on Invertible grounds
%From this set, we know that every invertible subset of the original 9 %vectors (the columns of Dt) must also be invertible after Dt has been acted on by P. This is because the product of two invertible ma
%invertible
possib=nchoosek(9,4);%The amount of ways that one can make a 4x4 matrix from 9 columns
possib list=nchoosek(1:9,4);%The combinations of columns to make a 4x4 matrix
for n=1:possib
       check=Dt(:,possib_list(n,:));
      if rank(check) == 4*If it is invertible we increase our count
    count=count+1;
      end
inv_num=count;
inv_list=zeros(inv_num,4);%Preallocate the space for the lists of combinations of columns that are invertible.
count=0;
      check=Dt(:,possib list(n,:));
      if rank(check) == 4
count=count+1;
            inv_list(count,:) = possib_list(n,:); % Stores the combination of columns that are invertible
      end
end
%Now that we know which combinations of columns are invertible in our %original matrix, we check to see if the SAME combination of columns is %invertible within our list of candidate matrices.
count=0:
for k=1:second_filter_num
      flag=0;
            c=1:inv_num
            mat=second_filter(:,inv_list(c,:),k); % Selects the combination of columns that should be invertible
            if rank(mat) ~= 4% If this is not invertible, we flag.
                  flag=1;
            end
       end
      if flag==0%If each combination is invertible, we add it to our count
      end
third_filter_num=count; third_filter_num));%Preallocate our space and run the loop once more to store the information
count=0;
for k=1:second_filter_num
       flag=0;
      for c=1.inv num
             mat=second_filter(:,inv_list(c,:),k);
            if rank(mat)~=4
                   flag=1;
            end
      end
       if flag==0
             count=count+1:
             third_filter(:,:,count)=second_filter(:,:,k);
      end
%% 10. And now we filter among the combinations that cannot have at most 1 positive and at most 1 negative value in each column
%The general idea is that we will go through each column and make a
%"relationship" between pairs of entries in each column and make a %"relationship" between pairs of entries in each column. For instance, %if one column is [0,p2\_2,0,p4\_4]', we know that p2\_2 and p4\_4 must have %opposite signs (if one is positive, the other is negative). If the column %was rather [0,p2\_2,0,-p4\_4], we would then know that p2\_2 and p4\_4 have the %same sign (both are positive or both are negative).
%We build these relationships for each column and see if there is a contradiction.
%For example, imagine that our 4x9 matrix includes the following column vectors:
             [0,p2_2,0,p4_4]'
[0,0,p3_3,p4_4]'
                                                  (1)
                                            (2)
             [0,p2_2,p3_3,0]'
From (1) we know that p2_2 and p4_4 are of opposite sign. From (2) we know that p3_3 and p4_4 are of opposite sign. We then have a contradiction in (3) as an p4_3 are of opposite sign, and yet (1) and (2) combined say that p2_2 and p3_3 wast be of the same sign. This sort of contradiction provides the foundation for our final filter.
%We first make sure that there are 2 entries in each column that are not formally zero. We %do not in fact need two non-formally zero entries in each column, but a %"relationship" can only be formed when there are two non-formally zero entries. It could %be the case that there are 3 symbolic zeros, but as it so happens, after %all of the filtering it is the case that we have exactly two entries that %are formally zero. We show this here:
```

```
check=0;
 for n=1:third_filter_num
          for j=1:9
                   nz num=length(find(third_filter(:,j,n)));%counts the zeros in the column if nz_num-=2%If we do not have two entries formally set to zero:
                            check=check+1;
                  end
         end
end
 %As one can see, check == 0 such that we have exactly two non-formally zero entries
A second check that we will have to make (to ensure that the next loop is specified correctly) is to make sure that we do not have pi_4's alone in a scolumn where we do not know whether or not it is NZ. As we add relationships based on having the same or opposite sign, we want to make
 %sure that we do not make a comparison with pi 4 when it may be zero.
 check2=0;
 for k=1:third_filter_num
         flag=0;
for j=5:9
for i=1:4
                            str=char(third\_filter(i,j,n)); \$ As \ before, \ we string the entries and inspect the last character. \\ len=length(str); \$ Store the location of the last character
                             if len<664len>1%If the length is greater than 1 such that it is not "0" and less than 6 such that it is a single element ()
                                                if third_filter(i,j,n)~=third_filter(i,4,n)%Such that whether pi_4=0 is then unknown
                                                          flag=1;
                                      end
                 end
end
          end
          if flag==1
                   check2=check2+1;
          end
 end
*As we can see, check2==0. Therefore, we do not have any indeterminate *pi_4's. All the pi_4's that are alone in a column will be definitively NZ.
flag=0;%Will flag on if we have a contradiction
         opps_n=0;%The count of opposite relations
same_n=0;%The count of same relations
          for \overline{j}=1:9
                   j=::9
indx=find(third_filter(:,j,n)~=0); %We find all of our nonzero entries
str1=char(third_filter(indx(1),j,n)); %We string each entry
str2=char(third_filter(indx(2),j,n));
if length(str1)+length(str2)==9 %With a length of nine, we know that only one of the entries has a negative sign in front
                             Length(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-rength(Stif)-reng
                   elseif length(str1)+length(str2)==8||length(str1)+length(str2)==10
%If the length is 8, neither element has a negative sign. If it
%is 10, they both have a negative sign. Either way, we know
                              %that the elements then must be of OPPOSITE sign
                             opps n=opps n+1;
                             opps(opps_n,:)=[third_filter(indx(1),j,n),third_filter(indx(2),j,n)];
          end
          %Now we clean so that we do not get negative signs in front of elements
         for i=1:same_n
  for j=1:2
    negcheck=char(same(i,j));
                            if length(negcheck) == 5
    same(i,j) = (-1) *same(i,j);
                             end
                   end
          end
          for i=1:opps_n
for j=1:2
                             negcheck=char(opps(i,j));
                             if length (negcheck) == 5
                                       opps(i,j)=(-1)*opps(i,j);
                             end
                   end
          end
          %Now we do a first check to see whether or not there will be any
          %contradictions directly
          flip=[opps(:,2),opps(:,1)]; % also check the flip as p1_1, p1_2 would be the same as p2_1, p1_1
         check=intersect(same,opps,'rows');
check2=intersect(same,flip,'rows');
if ~isempty(check)||~isempty(check2)
                   *If the intersection of the same and opposite relation is non-empty %such that a pair of elements is said to have both the same and %opposite sign, we know this matrix fails.

flag=1; %And then we will skip the next loop and move on to the next matrix.
          %We will now add to our list of same/opposites via transitivity
          | Non_count=1;
| %The loop_count will count the number of times that we cycle through
| %our same and opposite lists, adding new relationship via transitivity.
         %We have an arbitrary limit on the loop count so that we do not loop %indefinitely if there was some error prior.

while flag==0&&loop_count<5
for i=1:length(opps)-1
```

```
%As we will look at occurences of a selected element later in
                %the same and opposite lists, we do not look for more %occurences when we are at the end of the list.
                for j=1:2
                     search=opps(i,j);
                     %'Search' is the first element and we will look for more
                     %occurences of this element down the list in opposite and %same. 'Pairing' is the element that we know has an
                     %opposite relationship with 'search'.
                          pairing=opps(i,2);
                     pairing=opps(i,1); end
                     newopps=opps((i+1):length(opps),1:2); % Searches down the list from where we are currently
                    same=[same;new rels];%As the opposite of opposite is same, we add to our same list.
                     if ~isempty(r1)%if we find an entry down the same list...
                          \label{lem:new_rels=sym} new\_rels=sym(zeros(length(r),2)); $$Then the new relations that we make will be added to opposite. for b=1:length(r1)
                               if c1(b) == 2
                                     \label{eq:continuous} \begin{array}{l} \text{new\_rels}\,(b,1:2) = [\text{pairing,same}\,(\text{r1}\,(b)\,,1)\,]\,; \$stores \ the \ new\ relationship \\ \end{array}
                               else
                                     new_rels(b,1:2) = [pairing, same(r1(b),2)];
                          end
                          opps=[opps;new_rels];%As the opposite sign of the same sign is opposite, we add to our opposite list.
                    end
               end
          flip=[opps(:,2),opps(:,1)];%We flip the list again before checking intersections
          check=intersect(same,opps,'rows');
          Check-Intersect(same,filp,'rows');

if ~isempty(check) || ~isempty(check2)

%If the intersection of the same and opposite relation is non-empty
%such that a pair of elements is said to have both the same and
%opposite sign, we know this matrix fails.
               flag=1;
          loop_count=loop_count+1;
     end
     if flag==0%if we looped through 5 times and still were not able to find a contradiction..
    candidate_matrix=n;
    disp('Error: Matrix #n was not thrown out of consideration');
          *Therefore, if there is a printed message, we know that we were 
%unable to throw out the n'th matrix in third_filter.
end
```